ECON 2B03 Summary

Author: Kemal Ahmed

Instructor: Dr. Cameron Churchill

Date: Winter 2014

*Math objects made using* [*MathType*](http://www.dessci.com/en/products/mathtype/)*; graphs made using* [*Winplot*](http://math.exeter.edu/rparris/winplot.html)*.*

Please join GitHub and contribute to this document. There is a guide on how to do this on my GitHub.

Table of Contents

[Week 1 − Sustainability 2](#_Toc381294247)

[Triple-Bottom Line 2](#_Toc381294248)

[Seven Revolutions 2](#_Toc381294249)

[Week 2 3](#_Toc381294250)

[Methods of Interest Calculation 4](#_Toc381294251)

[Lump Sum 4](#_Toc381294252)

[Simple Interest 4](#_Toc381294253)

[Compound Interest 4](#_Toc381294254)

[Continuous Compound 5](#_Toc381294255)

[Cash Flow Diagrams 5](#_Toc381294256)

[Week 3 6](#_Toc381294257)

[Equivalence 6](#_Toc381294258)

[Compound Interest Factors 6](#_Toc381294259)

[Compound Amount Factor 6](#_Toc381294260)

[Present Worth Factor 7](#_Toc381294261)

[Sinking Fund Factor 7](#_Toc381294262)

[Uniform Series Factor 7](#_Toc381294263)

[Capital Recovery Factor 7](#_Toc381294264)

[Series Present Worth Factor 7](#_Toc381294265)

[Week 4 7](#_Toc381294266)

[Growth-Adjusted Interest Factors 7](#_Toc381294267)

[Arithmetic Gradient Series Factor 7](#_Toc381294268)

[Arithmetic Gradient Series Factor 8](#_Toc381294269)

[Week 5 9](#_Toc381294270)

[Coupon Rate 9](#_Toc381294271)

[Bond 9](#_Toc381294272)

[Week 8 10](#_Toc381294273)

# Week 1 − Sustainability

**model**: an simplification of reality that captures information useful and appropriate for a specific purpose

**linear product lifecycle**: energy in and out at every stage



**closed-loop product lifecycle**: recycling, re-use, energy only lost at consumer level



**Ingenuity Gap**: the gap between requirements and solutions, which is caused by an increasing complexity (?)

## Triple-Bottom Line

Focuses on:

* **Social sustainability**: productive service to society
* **Environmental sustainability**: resources/land
* **Economic sustainability**: cost efficient

## Seven Revolutions

1. Markets: compliance to competition
2. Values: hard to soft
3. Transparency: closed to open
4. Life-cycle Technology: product to function
   1. Companies responsible for entire product life-cycle
5. Partnership: subversion to symbiosis
   1. Companies cooperate
6. Time: wider to longer

# Week 2

**Cash-flow period**: time over which you are calculating effective interest rate

**Interest** [*I*]: compensation for giving up the money

**Annual interest rate** [*r*]: nominal interest rate over one year

**Present worth** [*P*]:

* The amount of money that is currently being dealt with (whether being loaned, or an annuity)
* Before initiating a time period exchange, the present worth is known as the **principle amount**
* Trying to bring all arrows on cash flow diagram to 0 (one period before the first payment)

**Future Worth** [F]: the future value of the time period exchange

**Interest period** [*m*]: interest compounds per year (not cashflow periods)

**Cash flow period (cfp)**:or *payment period* is how long it is between your payments

Don’t forget that there are 4 quarters in a year and 3 months in a quarter-year.

**Interest rate per cfp** [*i*]: interest for each interest period 

**Number of compounds per cfp** [*k*]: should never be a fraction

My way of calculating it is:

**Effective Interest rate** [ie]: overall interest rate that takes compounding and payment periods into consideration



**Effective interest per cash flow** [ie/k]: 

Your effective interest rate should be close to nominal interest rate/cash-flow periods per year.

## Methods of Interest Calculation

* [Lump Sum](#_Lump_Sum)
* [Simple Interest](#_Simple_Interest)
* [Compound interest](#_Compound_Interest)

### Lump Sum

**Lump sum**: one payment at the end of the time period exchange covers all the funds borrowed, so there is only one interest calculation. The interest on a lump sum does not change over time, but simply the amount paid.





### Simple Interest

**Simple interest**: a method of calculating interest that is based off the time it takes to pay off the loan and the principle amount



### Compound Interest

**Compound interest**: a method of calculating interest that charges interest on the principle as well as unpaid interest each “compound”



With compound interest comes a **compound period**, which is the amount of time, until interest begins to be charged on unpaid charges on top of previous unpaid interest. Compounding periods are assumed to have equal length.



### Continuous Compound



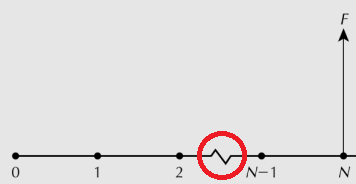
## Cash Flow Diagrams

Cash flow diagrams are graphical representations of a system that aid in analysis of cash flows

Since each cash flow is paid as an impulse, instead of continuous outflow from an account, the cash flows are represented by arrows, which can be positive (up) or negative (down) on a chart where time is along the y-axis (represented horizontally) and the cash flow is represented along the x-axis (represented vertically)



Sometimes when there are repeated points, with the same value, we represent the area with repeated points with a *squiggle* on the cash flow diagram:



**Linear Interpolation**: using 2 different *i*’s: one that’s bigger than the desired one and one that’s smaller than the desired one



Sometimes you can approximate to i = r/m

actually, your x’s are i’s in this case (change that)

y’s are your annuities

y2 would be your given A at given N and a guessed (upper bound) x2 and y1 would be the A at the point in the table at your given N and x1.

?

# Week 3

## Equivalence

**Equivalence**: when the value of something is the same at the one period as at a different period, which is determined by the interest rate

* **Mathematical**: comparing future to present by a factor of *time*
* **Decisional**: comparing future to present by a factor of *periods*
* **Market**: (?)

Note: a payment at time 0 can be assumed to occur at the end of the previous period

## Compound Interest Factors

A/B: A given B; A is unknown, B is known

**Number of payments** [*N*]: total periods − first payment + 1[interest begins from day one, payment does not];

Number of arrows on cash-flow diagram

### Compound Amount Factor





### Present Worth Factor



### Sinking Fund Factor



### Uniform Series Factor



### Capital Recovery Factor





**Salvage value** [*S*]: value after process is complete (usually 0)

### Series Present Worth Factor



# Week 4

## Growth-Adjusted Interest Factors

### Arithmetic Gradient Series Factor

**Base payment of Annuity** [*A'*]

**Nominal increase of an annuity** [*G*]: also known as gradient



A': base annuity cost





|  |  |
| --- | --- |
| **Cases** | **Meaning** |
| A > 0, G > 0 | Positive annuity, increasing cash flow |
| A > 0, G < 0 | Positive annuity, decreasing cash flow |
| A < 0, G > 0 | Negative cash flow, decreasing magnitude |
| A < 0, G < 0 | Negative cash flow, increasing magnitude |

Remember that the first compounding period has G = 0

## Arithmetic Gradient Series Factor

**Percentage Increase of an Annuity** [*g*]

**Growth-adjusted interest rate** [i°]: 





|  |  |  |
| --- | --- | --- |
| **Cases** | **Meaning** | **Procedure** |
| i > g > 0 | Positive *growth*, but  decreasing *interest rate*, so  *i0* is positive | Use tables or formulas |
| g > i > 0 | Positive *growth*, but  increasing *interest rate*, so  *i0* is negative | Use formulas only |
| g = i > 0 | *Growth* = interest rate, so  *i0* is zero |  |
| g < 0 | Negative *growth*, so  *i0* is positive | Use tables & formulas |

**Discrete Model**: cash flows occur at the end of periods

**Continuous Model**: compound continuously over time

Long-lived projects:

**Amortization**: number of years it would take to repay a mortgage loan in full for a given interest rate and payment schedule

**Term**:

**Mortgage**:

P = Total – Down



The default for car loans and mortgages is to convert the interest rate into monthly compounding from annual

How much of a given payment, M, within an annuity is interest: (value of annuity) – (FN−1 – FN)

# Week 5

## Bond

**Bond**: issuer of a bond takes a loan from the investor

* **purchase price**: amount “lent”
* **going interest rate**: interest rate of
* **par**/**face value**: total nominal amount the issuer will have given back to the investor
  + the difference between this and purchase price depends on the going interest rate (≠ coupon rate)
* **coupon rate**: the annual percentage of the par value that the issuer pays the investor, similar to monthly mortgage payments
  + The default frequency for payments is semi-annually (i.e. every 6 months), so i = r/2
* **maturity date**: set end date of loan
* a type of fixed-income security, since you know how much you’ll get back
* useful if fluctuating stock market

The coupon rate is stated for the year, but you need to cut that by how many times (multiply by face value/times received) you get the coupon, just as you need to cut down your nominal interest by number of compounds for any other interest

Comparison Methods:

* **PW Method**: examine present worth of all project cash flows
* **AW method**: convert all cash flows to annuities

**Assumptions**:

1. Costs & benefits are always measurable by money
2. Future cash flows are known with certainty
3. Cash flows are unaffected by inflation/deflation
4. Sufficient funds are available
5. Taxes are not applicable
6. Down payments ≤ proceeding cash flows

**Fixed rate**: fixed as a percentage of par value

**Floating rate**: adjustable interest payments

**Minimum Acceptable Rate of Return** (MARR): an interest rate that must be earned for a project for it to be worthwhile; would have to be larger for tech companies, since they can’t afford to stretch projects over longer periods of time

You want the thing with the greatest present worth (PW)

If you need to compare to figure out which is the best option, doing an annual worth will save time because you only have to calculate for one year.

# Week 8

